

August 2012

Bachelor of Computer Application (BCA) Examination
II Semester**Mathematics - II**

Time : 3 Hours]

[Max. Marks : 40

Note : All questions are compulsory and carry equal marks. Solve any two parts from each question.

1. (a) Trace the curve $x^3 + y^3 = 3axy$.

- (b) Test the convergence of :

$$\int_0^{\pi/2} \log \sin x \, dx .$$

- (c) Trace the curve $r^2 = a^2 \sin 2\theta$.

2. (a) Prove that : $\sqrt{1/2} = \sqrt{\pi}$.

- (b) Prove that :

$$\int_0^{\infty} \frac{x^c}{c^x} \, dx = \frac{\sqrt{c+1}}{(\log c)^{c+1}}, c > 1.$$

- (c) Prove that intrinsic equation of the parabola $3ay^2 = 2x^3$ is $9s^2 = 4a(\sec^2 \Psi - 1)$.

3. (a) Evaluate : $\int_0^1 \int_0^1 \int_0^1 e^{x+y+z} \, dx \, dy \, dz$.

- (b) If $\vec{r} \times d\vec{r} = \vec{0}$ then show that $\hat{z} \cdot \vec{r} = \text{constant}$.

- (c) Verify Stokes theorem for $\vec{F} = (x^2 + y^2) \mathbf{i} - 3xy \mathbf{j}$ taken rounded the rectangle bounded by $x = \pm a$, $y = 0$, $y = b$.

4. (a) If $u = \log \frac{x^4 + y^4}{x + y}$ then prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 3$.

- (b) Investigate the continuity of the function :

$$f(x, y) = \begin{cases} \frac{xy^2}{x^2 + y^2}; & (x, y) \neq (0, 0), \\ 0; & (x, y) = (0, 0) \end{cases}$$

- (c) State and prove mean value theorem for a function of two variables.

5. (a) Find the maximum and minimum value of the function

$$f(x, y) = xy(a - x - y).$$

- (b) Find the maxima and minima of

$$u = x^2 + y^2 + z^2 \text{ where } ax^2 + by^2 + cz^2 = 1.$$

- (c) Test the convergence of the series :

$$\frac{x}{1.2} + \frac{x^2}{2.3} + \frac{x^3}{3.4} + \frac{x^4}{4.5} + \dots \text{ where } x > 0.$$

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